CaTTS: Calendar Types and Constraints for Web Applications

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ABSTRACT

Data referring to cultural calendars such as the widespread Gregorian dates but also dates after the Chinese, Hebrew, or Islamic calendars as well as data referring to professional calendars like fiscal years or teaching terms are omnipresent on the Web. Formalisms such as XML Schema have acknowledged this by offering a rather extensive set of Gregorian dates and times as basic data types. This article introduces into CaTTS, the <u>Calendar and Time Type System</u>. CaTTS goes far beyond predefined date and time types after the Gregorian calendar as supported by XML Schema. CaTTS first gives rise to *declaratively specify* more or less complex cultural or professional calendars including specificities such as leap seconds, leap years, and time zones. CaTTS further offers a tool for the static type checking (of data typed after calendar(s) defined in CaTTS). CaTTS finally offers a language for *declaratively expressing* and a solver for effi*ciently solving* temporal constraints (referring to calendar(s) expressed in CaTTS). CaTTS complements data modeling and reasoning methods designed for generic Semantic Web applications such as RDF or OWL with methods specific to the particular application domain of calendars and time.

Categories and Subject Descriptors

I.2.4 [Artificial Intelligence]: Knowledge Representation Formalisms and Methods—*representation languages*; D.3.1 [Programming Languages]: Formal Definition and Theory—*syntax*

General Terms

Languages

Keywords

time, calendars, types, Web reasoning

1. INTRODUCTION

Data referring to cultural calendars such as the widespread Gregorian dates but also dates after the Chinese, Hebrew, or Islamic calendars as well as data referring to professional calendars like fiscal years or teaching terms are omnipresent on the Web. Most likely, they will play an essential role on the Semantic Web, too. Formalisms such as XML Schema have acknowledged this by offering a rather extensive set of Gregorian dates and times as basic data types.

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	CaTTS	
CaTT	CaTTS-CL	
CaTTS-TDL	CaTTS-FDL	

Figure 1: Languages of CATTS.

This article introduces into CaTTS, the <u>Calendar and</u> <u>Time Type System that goes far beyond predefined date</u> and time types after the Gregorian calendar. CaTTS consists of two languages, a *type definition language*, CaTTS-DL, and a *constraint language*, CaTTS-CL, of a (common) parser for both languages, and of a language processor for each language.

Using the (type) definition language CaTTS-DL, one can specify in a rather simple manner more or less complex, cultural or professional calendars [3]. Specificities like leap seconds, leap years, and time zones can be easily expressed in CaTTS-DL. Calendars expressed in CaTTS-DL are composable in the sense that the language offers a means for modules. Thus, one can extend a standard calendar such as the Gregorian calendar used in Germany with a particular teaching calendar, e.g. the one of a specific German university.

CaTTS-DL gives rise to defining both, calendric data types specific to a particular calendar – such as "working day", "Easter Monday", "exam week", or "CS123 lecture" (defining the times when the Computer Science lecture number 123 takes place) – using the language fragment CaTTS-TDL (for <u>Type D</u>efinition <u>L</u>anguage) of CaTTS-DL, and data formats for such data types – such as "5.10.2004", "2004/10/05", or "Tue Oct 5 16:39:36 CEST 2004" – using the language fragment CaTTS-FDL (for <u>F</u>ormat <u>D</u>efinition <u>L</u>anguage) of CaTTS-DL.

The language processor for CaTTS-DL consists of two software components, a *static type checker* and a *predicate interpreter*. Consider a calendar C specified in CaTTS-DL and a program P in the language CaTTS-CL, XQuery, XSLT or any other program P with type annotations referring to types and/or formats specified in the calendar C. CaTTS' static type checker verifies and/or extends the type annotations in P generating a type checked version P' of P:



Consider a type definition T (e.g. "working day" or "exam week") from a calendar specified in CaTTS-DL and a data item D (e.g. "2004/10/05"). CaTTS' predicate interpreter detects whether the data item D has type T (e.g. whether "2004/10/05" is a "working day" or an "exam week" - the later being probably false):



Both CaTTS-DL and CaTTS-CL provide (the same) predefined functions (e.g. shift forward and backward, during, and usual arithmetics). Using these functions, one can express for example, "the second day after working day X" (in CaTTS: shift X:working_day forward 2 day).

CaTTS' type checker can be used for static type checking of programs or specifications in *any* language (e.g. XQuery, XSLT, XML Schema), using date formats enriched with type annotations after some calendar specified in CaTTS-DL. In particular, it is used for the static type checking of temporal constraint programs in CaTTS-CL, the constraint language of CaTTS.

Using CaTTS' constraint language CaTTS-CL, one can express a wide range of temporal constraints referring to the types defined in calendar(s) specified in the definition language CaTTS-DL. For example, if one specifies in CaTTS-DL a calendar defining both, the Gregorian calendar (with types such as "Easter Monday" or "holiday") and the teaching calendar of a given university (with types such as "working day", "CS123 lecture", and "exam week"), then one can refer in CaTTS-CL to "days that are neither holidays, nor days within an examination week" and express constraints on such days such as "strictly after Easter Monday and before June". Thus, using CaTTS-CL one can express real-life, Web, Semantic Web, and Web service related problems such as searching for train connections or making appointments (e.g. for audio or video conferences) over several time zones.

CaTTS provides with a constraint solver for problems expressed in CaTTS-CL. This solver refers to and relies on the type predicates generated from a calendar definition in CaTTS-DL. This makes search space restrictions possible that would not be possible if the calendar and temporal notion would be specified in a generic formalism such as first-order logic and processed with generic reasoning methods such as first-order logic theorem provers.

2. CATTS AND THE SEMANTIC WEB

CaTTS complements data modeling and reasoning methods such as RDF [15] or OWL [14] designed for *generic* Semantic Web applications with methods *specific* to a particular application domain, that of calendars and time. CaTTS approach is a form of "theory reasoning" like "paramodulation". Like paramodulation ensures natural expressing and efficient processing of equality in resolution theorem proving, CaTTS makes a user friendly expression and an efficient processing of calendric types and constraints possible. CaTTS departs from time ontologies such as the DAML Ontology of Time [4] or time in OWL-S [10] as follows:

- CaTTS considerably simplifies the modeling of specificities of cultural calendars (such as leap years, sunbased cycles like Gregorian years, or lunar-based cycles like Hebrew months),
- CaTTS provides both, a static type checker and type predicates for every CaTTS calendar(s) specification,
- CaTTS comes along with a constraint solver dedicated to calendar definitions that (1) processes CaTTS type annotations as constraints and (2) the language of which is amenable to CaTTS static type checking.

3. CATTS' MODEL IN A NUTSHELL

This section is a mathematical prologue that can be skipped in a first reading.

CaTTS' notion of time is *linear*. CaTTS is not intended for expressing possible futures, hence it is not based on a "branching time". Most common-sense, Web and Semantic Web and many Web service application can be conveniently modeled in a linear time framework.

CaTTS' notion of time is purely *interval-based*, i.e. temporal data of every kind have a duration. This reflects a widespread common-sense understanding of time according to which one mostly refer to time interval, not to time points. E.g. one refers to "2004/10/05", a day, or to "1st week of October 2004", a week. Even time point-like data such as 9:25 can be perceived as having a duration, possibly as small as one second or one millisecond. Considering only time intervals and no time points has two advantages. First, it significantly simplifies data modeling, an advantage for CaTTS' users. Second, it simplifies data processing, i.e. static type checking and constraint reasoning, an advantage for CaTTS' language processors. However, CaTTS can deal with time point-like data like the beginning of a week or whether a day d falls into a week w or not, as well.

In order to *formalize* CaTTS (time point-less) model, however, time points have to be considered:

Definition 1. A base time line is a pair $(\mathcal{T}, <_{\mathcal{T}})$ where \mathcal{T} is an infinite set (isomorphic to \mathbb{R}) and $<_{\mathcal{T}}$ is a total order on \mathcal{T} such that \mathcal{T} is not bounded for $<_{\mathcal{T}}$. An element t of \mathcal{T} is called **time point**.

Each CaTTS type definition creates a *discrete* image of the time line since CaTTS data types define data items with durations. E.g. data types "day" and "working day" imply two (different) images of the time line: days partition the time line, working days correspond to a portion of the day partition of the time line. Both images of the time line are discrete, i.e. isomorphic to \mathbb{Z} . The notion of *time granularity* [2] formalizes such "discretizations" of the time line:

Definition 2. Let $(\mathcal{T}, <_{\mathcal{T}})$ be a base time line. Let $G = \{g_i \mid i \in \mathbb{Z}\}$ be a set isomorphic to \mathbb{Z} . Let's call the elements of G granules. A time granularity is a (non-necessarily total) function \mathcal{G} from G in the set of intervals over \mathcal{T} such that for all $i, j \in \mathbb{Z}$ with i < j

- 1. if $\mathcal{G}(g_i) \neq \emptyset$ and $\mathcal{G}(g_j) \neq \emptyset$, then for all $t_i \in \mathcal{G}(g_i)$ and for all $t_j \in \mathcal{G}(g_j)$ $t_i <_{\mathcal{T}} t_j$.
- 2. If $\mathcal{G}(q_i) = \emptyset$, then $\mathcal{G}(q_j) = \emptyset$.

Examples of granules are days, working days, weeks, months, holidays, etc. According to Definition 2, two different granules of a same time granularity do not overlap. The first condition of Definition 2 induces from the ordering of the time points (of the base time line) the common-sense ordering on granules: e.g. the day "10/25/2004" is after the day "10/24/2004". The second condition of Definition 2 is purely technical: it makes it possible to refer to the *infinite* set Z also for *finite* sets of granules (e.g. someone's exam days during his/her years of study).

Definition 3. Let \mathcal{G} be a time granularity and $g_i, g_j \in \mathcal{G}$ granules.

A duration D over \mathcal{G} is a number (expressed as an unsigned integer) of granules of \mathcal{G} .

Thus, a duration can be informally understood as a time interval over a granularity with a given length but with no specific starting or ending point.

Subtypes are defined in CaTTS in terms of either *inclusion* or *aggregation* of time granularities. E.g. a type "working day" is an inclusion (in the common set-theoretic sense) of the type "day" since the set of working days is a subset of the set of days; the type "week" is an aggregation (in constructive set-theory) of the type "day" since each week can be defined as a time interval of days.

Definition 4. Let \mathcal{G} and \mathcal{H} be time granularities. \mathcal{G} is an **aggregation subtype of** \mathcal{H} , denoted $\mathcal{G} \preceq \mathcal{H}$, if every granule of \mathcal{G} is an interval over \mathcal{H} and every granule of \mathcal{H} is included in (exactly) one granule of \mathcal{G} .

Definition 5. Let \mathcal{G} and \mathcal{H} be time granularities. \mathcal{G} is an **inclusion subtype of** \mathcal{H} , denoted $\mathcal{G} \subseteq \mathcal{H}$ if every granule of \mathcal{G} is a granule of \mathcal{H} .

The two subtype relations, inclusion subtype and aggregation subtype, are corner stones of CaTTS that, to the best of the knowledge of the authors, have not been proposed elsewhere. As the examples given below show, they are very useful in modeling calendars. Indeed, they reflect widespread forms of common-sense reasoning with calendric data.

Note that $\leq \cup \subseteq$ is an order relation on time granularities. $\leq \cup \subseteq$ is defined as follows: $\mathcal{G}_1 \leq \cup \subseteq \mathcal{G}_2$ iff $\mathcal{G}_1 \leq \mathcal{G}_2$ or $\mathcal{G}_1 \subseteq \mathcal{G}_2$. The following formalization of the notion of "calendar" reflects the central role played by aggregation and inclusion subtyping in CaTTS:

Definition 6. A calendar $C = \{\mathcal{G}_1, \ldots, \mathcal{G}_n\}$ is a finite set of time granularities such that there exists a $\mathcal{G}_i \in C$ and for all $\mathcal{G}_j \in C$, $i, j \in \{1...n\}$ and $i \neq j \ \mathcal{G}_j$ is $\leq \bigcup \subseteq$ -comparable with \mathcal{G}_i .

The subsequently illustrated set of time granularities defines a calendar; each of the time granularities is $\leq \cup \subseteq$ -comparable with the time granularity "second".





Figure 2: Indexing of the types defined in Section 4 (day(1)) is Thursday, January 1, 1970).

4. CATTS-DL: DEFINITION LANGUAGE

Recall that CaTTS' definition language, CaTTS-DL, consists of a type definition language, CaTTS-TDL, and a date format definition language, CaTTS-FDL.

CaTTS-TDL provides a set of type constructors for declaring time granularities as subtypes (of predefined or userdefined) types in terms of *predicates*, called *predicate subtypes*. A subtype in CaTTS specifies (in terms of a predicate) a set, referred to as "predicate set". The usual settheoretic operations (e.g. \cup) can be applied to predicate sets. In CaTTS, calendars (cf. Definition 6) are themselves typed by *calendar signatures*. This makes CaTTS calendar specifications reusable, maintainable, and easy to extend. In addition, user-definable *calendar functions* can be specified in CaTTS that parameterize calendars. Such functions provide a means to specify different calendar versions all having the same calendar signature. CaTTS-FDL provides a means to specify specific constants, i.e. the data items of predicate subtypes defined in a CaTTS-TDL calendar definition.

4.1 **Reference Time**

Each CaTTS implementation has a single predefined (base) type called reference.¹ reference is a time granularity such as "second" or "hour", chosen e.g. depending on the operating system. If the type reference is used in a CaTTS-DL calendar specification, then all other (user-defined) types are expressed directly or indirectly in terms of reference, using CaTTS' aggregation and/or inclusion subtyping (cf. Section 3). Note that the use of reference is optional in some CaTTS-DL calendar specification. If reference is e.g. the time granularity "second", a convenient choice with the Unix operating system, then one can specify (using CaTTS-DL) further coarser time granularities such as "day", "week", and "year" as well as finer time granularities such as "millisecond". The reference type makes conversions among any other types defined in a CaTTS-DL calendar specification (in terms of aggregation and/or inclusion), and, thus, between different CaTTS-DL calendars possible.

In CaTTS' prototype implementation, **reference** is the time granularity "second" of Unix (UTC seconds with midnight at the onset of Thursday, January 1 of year 1970 (Gregorian) as fixed point indexed by 1).

In CaTTS-DL, one defines a type finer than that of **reference** as follows:

type millisecond = refinement $1000 @ reference(1);^2$

The type (time granularity) millisecond is defined as a thousandth refinement of a second (recall reference is the

¹**reference** is a base type, because it has no internal structure as far as the type system of CaTTS is concerned.

 $^{^2\}mathrm{In}$ this and the following examples, type identifiers start with lower case letters.

time granularity "second"). The type millisecond is anchored at (denoted @) second 1 (denoted reference(1)), since millisecond(1) is the first millisecond in the interval of milliseconds specifying the first second (i.e. reference(1)). Thus, in CaTTS types such as reference or millisecond induces clear integer indices of its data items. This indexing of data items turns out to be extremely useful in practice (cf. below).

4.2 Predicate Subtypes

Infinite sets are logically encoded by predicates: for any set A, the predicate $p : A \to \mathbb{B}$ defines the set of those elements of A that satisfy p. Such sets are called *predicate sets*. In type theory, predicate sets are interpreted as *predicate subtypes*, particularly used to express dependent function types [11]. CaTTS uses predicate subtypes in a different manner and not for theoretical, but instead practical purposes.

CaTTS uses predicate subtypes as a means to define calendric types. E.g. one can describe the time granularity "week" as the *subset* of those time intervals over the time granularity "day" having a duration of 7 days and beginning on Mondays. This can be directly expressed in CaTTS-DL as follows:

type week = aggregate 7 day @ day(-2);

The type week is an aggregation of days such that each data item is an interval with duration "7 days". The first week (i.e. week(1)) is anchored at (denoted @) day(-2), i.e. the first day of the interval of days *aggregated* to the data item week(1). Since day(1) is a Thursday (recall that CaTTS) implements Unix time with Thursday, January 1, 1970 as fixed point indexed by 1), day(-2) is a Monday. Any further index can be computed relative to this anchor (cf. Figure 2). Thus, the predicate subtype week:day $\rightarrow \mathbb{B}$ specifies the infinite set of those day time intervals satisfying the predicate "week" as previously expressed in CaTTS-DL. The type week is an *aggregation subtype* of the type day (cf. Definition 4), written week <: day in CaTTS' syntax, and read as "week is an aggregation of day". In CaTTS-DL, aggregation subtypes are constructed by the aggregate constructor, or by the predicates "# <" ("coarser restriction") and "#>" ("finer restriction"), set-based operations defined for CaTTS due to predicative set aggregation. E.g. aggregating the type weekend_day into the type week yielding the type weekend, a coarser restriction of week to weekend_day. The two set-based aggregation predicates may also be used to define types having non-convex data items like "working_week" (a coarser restriction of working days, i.e. days that are neither weekend days nor holidays, into weeks). Note that one might define aggregations having data items of different durations involving often complex conditions (e.g. Gregorian or Hebrew months), as well.

One can describe the time granularity "weekend day" as the *subset* of those granules of time granularity "day" that are either Saturdays or Sundays. This can be directly expressed in CaTTS-DL as follows:

The type saturday is a selection of the 6^{th} day relative in each week. Thus, the predicate subtype saturday:day $\rightarrow \mathbb{B}$

```
calendar type STD =
 sig
   type second;
   type minute
                        <: second;
   type hour
                        <: minute:
   type day
                        <: hour:
   type week
                        <: day;
   type month
                        <: day;
   type year
                        <: month;
   group day_of_week
                        c:
                           day;
   type weekend_day
                        c: day
   group holiday
                        c: dav:
 \mathbf{end}
```

Figure 3: Signature of a standard calendar in CaTTS-DL.

specifies the infinite set of those days satisfying the *predicate* "saturday" as previously expressed in CaTTS-DL. In the same manner, the type **sunday** is defined. Finally, the type weekend_day satisfies either the predicate of type saturday or (denoted "|") the predicate of type sunday. The types saturday, sunday, and weekend_day are inclusion subtypes of the type day (cf. Definition 5), written e.g. weekend_day c: day in CaTTS' syntax, and read as "weekend day is an inclusion of day". In CaTTS-DL, inclusion subtypes are constructed by the select constructor by specifying a predicate as a combination of any operation predefined in CaTTS (cf. Appendix A for the complete syntax of CaTTS) following the reserved word where, or by a set-based constructor: "|" ("or"), "&" ("and"), and "" ("except"), in fact ordinary set operations interpreted as predicate subtype constructors in CaTTS-DL. As illustrated in Figure 2, the indexing of inclusion subtypes is successive. The indexing of any inclusion subtype is however implicitly related to that of its inclusion supertype, appropriately choosing the data item indexed by 0 relative to that one of the supertype.

Note that weekend days may alternatively be defined as a group, i.e. a named collection of type definitions in CaTTS-DL:

```
group weekend_day =
  with select day(i) where (relative i in week)==j
  type saturday where j == 6
  type sunday where j == 7
  end
```

Having defined the group weekend_day, one can either referring to data items of the group weekend_day, or, more specific, to data items of one of the types (saturday, sunday) defined within the group, explicitly defined belonging to a less specific "kind", i.e. a group of a CaTTS' type.

Furthermore, CaTTS provides a *polytypic constructor*: $| \tau |$ (durations of τ) that describes for any type τ a duration (cf. Definition 3) whose data items are drawn from τ . For example, |day| is the type of durations of days.

Note that CaTTS' type constructors provide a natural way to obtain *periodic events*, e.g. the CS123 lecture offered within the summer term 2004 (referred to as ST04) (in CaTTS X:CS123_lecture during ST04) of type CS123_lecture. Note that periodic events are very frequently considered in current research. The authors believe that CaTTS offers a particularly convenient and intuitive manner to specify periodic events.

4.3 Calendar as Type

The basic entities of CaTTS-DL calendar definitions (cf.

Definition 6) are calendars, calendar signatures, and calendar functions.

4.3.1 Calendars

A calendar is a packaged, finite collection of CaTTS type definitions and calendar specifications, assigning types to type identifiers, groups to group identifiers, and calendars to calendar identifiers, similar to ML structures [9] or XML documents [13]. The types and calendars specified in a calendar are delimited by the keywords cal and end. The following specification binds a calendar to the identifier Cal. This calendar defines an environment mapping day, weeken-d_day, week, and weekend to their respective group and type definitions.

```
calendar Cal =
   cal
   type day;
   group weekend_day = with select day(i) where
      (relative i in week) == j
      type saturday where j == 6
      type sunday where j == 7
   end
   type week = aggregate 7 day @ day(0);
   type weekend = week #< weekend_day;
   end</pre>
```

Note that day is a user-defined reference type (isomorphic to the integers) without any further specifications. The identifiers in a calendar are qualified. For example, the qualified identifier Cal.week refers to the component week in the calendar definition Cal.

4.3.2 Calendar Signatures

Calendar signatures are kinds of "types" for calendars defined in CaTTS-DL, similar to ML [9] signatures or XML Schema declarations [12]. Calendar signatures specify identifiers and abstract predicate subtypes in terms of inclusion or aggregation supertypes for each of the components of a calendar implementing the signature. The following specification binds a calendar signature to the identifier SIG.

```
calendar type SIG =
   sig
   type day;
   group weekend_day c: day;
   type week <: day;
   type weekend c: weekend_day;
   end</pre>
```

This calendar signature describes those calendars having a type day, a group weekend_day, where each type belonging to must be an inclusion subtype of day and types week as aggregation subtype of day and weekend as aggregation subtype of weekend_day. Since the calendar Cal introduced above satisfies this calendar signature, it is said to *match* the calendar signature SIG. Note that a defined calendar usually matches more than one calendar signature, and vice versa, a calendar signature may be implemented by more than one calendar. Calendar signatures in CaTTS-DL may be used to define *views* of calendars due to *ascription*, i.e. specifying less components than implemented in any matching calendar. The non-specified components are thus local to its calendar specification.

4.3.3 Calendar Functions

Calendar functions are user-defined functions on calendars using a syntax similar to function declarations in many programming languages. A calendar function CF defining Hebrew weekend days can be declared in CaTTS as follows:

```
cal_fun CF(C:SIG):SIG =
cal
group weekend_day = with select C.day(i)
where (relative i in C.week) == j
type friday where j == 5
type saturday where j == 6
end
end
```

The calendar function CF takes as argument any calendar C matching the calendar signature SIG, and yields as result a calendar also matching SIG. When applied to a suitable calendar, the calendar function CF yields as result the calendar whose group weekend_day is that of (Hebrew) weekend days, i.e. Fridays and Saturdays. Furthermore, *any* type definition in C depending on that of weekend_day is changed respectively to the calendar function CF when applied to C. E.g. applying CF to the previously illustrated calendar definition Cal yields a "new" group weekend_day and the type weekend is changed, as well. Since the calendar function CF may be applied to *any* calendar matching the signature SIG, the function is polymorph, thus define a parameterized calendar.

4.4 CaTTS-FDL

With most applications, one would appreciate not to specify dates and times using indices of the data items of CaTTS types like day(23) or second(-123), but instead *date formats* like "5.10.2004", "2004/10/05", or "Tue Oct 5 16:39:36 CEST 2004". CaTTS-FDL provides a means for defining date formats.

A CaTTS-FDL date format is defined by a sequence of string constants and/or placeholders, the latter appearing as variable names optionally followed by a representation descriptor³. Consider the following example:

```
format stdfmt:day = y "-" m "-" d where
  stdfmt within year(y),
  stdfmt within M:month,
    m == relative index M in year,
    d == relative index stdfmt in month;
```

This CaTTS-FDL format specification binds the identifier stdfmt to a standard format for data items of type day. Both a parser and a render function (i.e. $String \rightarrow day$ as well as $day \rightarrow String$) can be computed by resolving the constraints associated with stdfmt. Given "1970-1-1", we get that y = 1970, m = 1 and d = 1 and can thus solve the constraints to get e.g. Gregorian.day(1). Vice versa, given (Gregorian.)day(1), we find that it is within year(1970), within M, which is equal to month(1) and is the 1st in a year, and that day(1) is the 1st in a month, yielding the same values for y, m and d as above.

Catalogs are collections of formats specifying to which calendar signature these formats can be applied. Such catalogs may be nested, applying to common scoping rules.

```
catalog ISO: STD =
    cat
    (* nested catalog for extended ISO formats *)
    catalog Extended =
        cat
        format stdfmt:day = y "-" m "-" d where
        stdfmt within year(y),
        stdfmt within M:month,
        m == relative index M in year,
        d == relative index stdfmt in month;
    end
end
```

³If none is given, that portion of the format is interpreted as a variable-length unsigned integer.

```
import LeapSeconds;
calendar Gregorian:STD =
 cal
   type second = reference;
   type minute = aggregate minute (i)
      alternate
         i = 1051200 (*1.1.1972*) -> 70 second
         hasLeapSec?(i)
                                       -> 61 second
        otherwise
                                       ->60 second
     end @ second(1);
   type hour = aggregate 60 minute @ minute(1);
   type day = aggregate 24 hour @ hour(1);
   type week = aggregate 7 day @ day(-2);
   type month = aggregate month(i)
      31 day named january,
     alternate
       |((i \ div \ 12) - 1970) \ mod \ 4 == 0 \ \&\&
        (((i \ div \ 12) - 1970) \ mod \ 100 \ != 0 \ ||
         ((i \text{ div } 12) - 1970) \mod 400 == 0) \longrightarrow 29 \text{ day}
       otherwise
                                              -> 28 \, day
     end named february
      31 day named march,
      30 day named april
      31 day named may,
      30 day named
                    june
      31 day named
                    july
      31 day named august
      30 day named september.
      31 day named october,
      30 day named november,
      31 day named december @ day(1);
   type year = aggregate 12 month (1);
   group day_of_week =
     with select day(i) where
  (relative i in week) == j
         type monday
                          where i
                                   == 1
         type tuesday
                          where
                                   == 2
                                 j
         type wednesday
                          where
                                   == 3
         type thursday
                          where
                                   -- 4
                          where j
         type friday
                                   == 5
         type saturday
                          where
                                   == 6
                                 j
                          where i = 7
         type sunday
     end
   type weekend_day = saturday | sunday
   group holiday = with select day(i) where
     (relative i in M) == j
     type all_saints where j == 2 for M = november
type christmas where j == 25 for M = december
    end
 end
```

Figure 4: The Gregorian calendar in CaTTS-DL.

As with calendars, identifiers defined within a catalog are qualified, e.g. ISO.Extended.stdfmt is the full name of the above format. Date formats specified in CaTTS-FDL may be imported into a program in the language CaTTS-CL, XQuery, or any other language using calendric data typed after CaTTS-DL calendar specifications by CaTTS' import mechanism for formats use_format.

4.5 Use Case: Specifying Calendars

To express and find solutions to real-life, Web, Semantic Web, and Web Service related problems such as train scheduling or making appointments, context-dependent semantics considering both cultural and professional calendars and time zones is necessary.

Consider the following scenario: A Munich-based business man needs to schedule a phone conference with a colleague in Tel Aviv. Besides the various constraints to schedule the phone conference, the business men use different calendars. Both use the *Gregorian* calendar to schedule everyday times and dates, but shifted according to different *time zones*. The Tel Aviv-based business man uses the *Hebrew* calendar for holidays to be considered, but, for the same reason, the Munich-based business man uses the Gregorian.

The CaTTS-DL calendar signature in Figure 3, assigned to the identifier STD, describes standard calendar types and groups matched by most calendars. **second** is a non-further specified type identifier.

The calendar definition given in Figure 4 binds a calendar to the identifier Gregorian such that this calendar must match the calendar signature STD (denoted Gregorian:STD). CaTTS allows for importing external libraries using the reserved word import. The calendar Gregorian imports a library LeapSeconds, containing, among other things, a boolean function hasLeapSec? over minutes. Leap second insertion into UTC-time (recall that reference is the time granularity of UTC-seconds) started in 1972 (Gregorian); 10 leap seconds have been inserted into the first minute of the year 1972. In the present CaTTS-DL modeling, the index of this minute is directly referred to. The type identifier second is assigned to the predefined base type reference. The rules for the Gregorian leap month February are expressed by a suitable combination of operations predefined in CaTTS. The predefined arithmetic function relative i in M (used in the group holiday) selects specific data items i of type day relatively located to each data item in type M, a local macro variable substituted by a CaTTS-DL type. Any further type definition is straightforward following the rules of the Gregorian calendar [5].

The calendar definition given in Figure 5 binds a calendar to the identifier Hebrew such that this calendar must match the calendar signature STD (denoted Hebrew:STD). The Hebrew day "23 Tevet 5730", a Wednesday (yom revii) is the day corresponding to the Unix epoch ("1 January 1970" (Gregorian)). To implement an alignment of Hebrew regaim⁴ and halaqim⁵ (Hebrew partitions of hours) with CaTTS' reference type a respective shift (denoted by the definition of **_ref**) is defined. The type identifiers second and minute are used to match the Hebrew calendar with the standard signature STD⁶. Note that Hebrew weeks start on Sundays (yom rishon), and that the first month in any He-

⁶Whether such an alignment of the Hebrew calendar to the

⁴Plural of rega.

⁵Plural of heleq.

brew year is Tishri. Since Hebrew leap year computations depend on the Metonic cycle aligning 19 sun-based years to 235 lunar-based months, the index 1 for Hebrew months is respectively moved form "Tevet 5730" to "Nisan 5720" by resetting this month's index (133) relatively to the index 1 (denoted ~@133). To simplify the modeling of the Hebrew calendar in CaTTS-DL, the library HebrewLeapYear, containing the various functions (e.g. isLeapAdarRishon? and isHebrewLeapYear?) used in the present calendar specification is imported. Such functions may however be directly specified within a CaTTS-DL calendar definition by a userdefined "macro". E.g. isLeapAdarRishon? (i.e. the second to last month in a Hebrew year which depends on the Metonic cycle) can be specified by the following two CaTTS-DL macros:

```
macro isLeapAdarRishonInCycle?(i) =
    i == 36 || i == 73 || i == 98 || i == 135
    || i == 172 || i == 209 || i == 234;
macro isLeapAdarRishon?(m) =
    isLeapAdarRishonInCycle?((m mod 235) + 1);
```

All rules implement in the CaTTS-DL definition of the Hebrew calendar are those suggested in [5].

Note that only a few Gregorian and Hebrew holidays are specified with the two present CaTTS-DL calendars. Further can be similarly specified in CaTTS-DL.

Since reference is UTC-time and since UTC-time is adjusted to the time zone Greenwich Mean Time (GMT), the previously mentioned calendars Gregorian and Hebrew correspond to this time zone. Any further calendar C matching also the calendar signature STD, but which refers to other time zones can be expressed by a (user-defined) calendar function, redefining the definition of type day by choosing suitable anchors for the considered time zones (cf. Figure 6). If the calendar function EET is applied to the calendar Gregorian or Hebrew, then any (aggregation or inclusion) subtype of day is respectively changed.

5. CATTS-CL: CONSTRAINT LANGUAGE

CaTTS-CL, CaTTS' constraint language, is statically typed after CaTTS-DL type definitions. CaTTS-CL is a language to declaratively express a wide range of temporal and calendric constraint problems. Such problems are then solved by CaTTS-CL's constraint solver. Given a CaTTS-DL specification of the Gregorian calendar (with types such as "weekend day") and the teaching calendar of a given university (with types such as "exam week"), one can refer in CaTTS-CL programs to weekend days. One can further express constraints on such days such as "after exam week" and "before June 2004" (assuming that the used date formats are specified in CaTTS-FDL). This problem is expressed in CaTTS-CL as follows:

X:weekend_day && X **after** Y:exam_week && X **before** "2004-06"⁷

The constraint variable X ranges over values of type weekend-_day and Y over exam_week. The constraints "after an examination week" (in CaTTS-CL X after Y:exam_week) and "before June 2004" (in CaTTS-CL X before "2004-06")

⁷In this and the following examples, constraint variables start with capital letters.

```
import HebrewLeapYear;
calendar Hebrew:STD =
 \mathbf{cal}
   type \_ref = refinement 114 @ reference(-43199);
   type second = aggregate 5 _ref;
   type rega = second;
   type minute = aggregate 76 second;
   type heleq = minute;
   type hour = aggregate 1080 minute;
   type day = aggregate 24 hour;
   type week = aggregate 7 day (-2);
   type month = aggregate month(i)
      30 day named nisan,
      29 day named iyyar.
      30 day named sivan,
      29 day named tammuz,
      30 day named av,
      29 day named elul
      30 day named tishri
      alternate
       | newYearDelay(i) == 2
         -> 30 day named long_marheshvan
otherwise -> 29 day named short_marheshvan
       end named marheshvan,
      alternate
       | newYearDelay(i) > 0
        -> 30 day named long_kislev
otherwise -> 29 day named short_kislev
      end named kislev,
      29 day named tevet
      30 day named shevat,
      alternate
       | isLeapAdarRishon?(i) -> 30 day
                                     named adar_rishon
       | otherwise none
      end,
      29 day named adar_sheni @ day(-21) ~@ 133;
   type adar = adar_rishon | adar-sheni;
   type year = aggregate
      alternate year(i)
        isHebrewLeapYear?(i) -> 13 month
         otherwise
                                  ->12 month
      end @ month(7) ~@ 5730:
   group day_of_week =
      with select day(i) where
(relative i in week) == j
         type yom_rishon where j == 1
         type yom_sheni where j == 2
         type yom_shelishi where j == 3
         type yom_revii where j == 4
         type yom_hamishi where j == 5
         type yom_shishi where j == 6
type yom_shabbat where j == 7
      \mathbf{end}
   type weekend_day = yom_shishi | yom_shabbat;
   group holiday = with select day(i) where
(relative i in M) == j
type yom_kippur where j == 10 for M = tishri
     type passover where j == 15 for M = nisan
    \mathbf{end}
 \mathbf{end}
```

Figure 5: The Hebrew calendar in CaTTS-DL.

(*CET: Central European Time, GMT + 1, Munich*)
calendar_function $CET(C:STD)$: $STD =$
cal
type day = aggregate 24 C. hour @ C. hour (2) ;
end
(*EET: Eastern European Time, GMT + 2, Tel Aviv*)
calendar_function EET(C:STD) : STD =
cal
type day = aggregate 24 C. hour @ C. hour (3);
end

Figure 6: Calendars in different time zones in CaTTS-DL.

STD calendar signature is appropriated or not, does not have to be discussed here. The present example aims at showing that it is possible and easy to express with CaTTS.

are straightforwardly expressed as illustrated. The constraints of CaTTS-CL are given in Appendix A.

CaTTS-CL provides function symbols for data items of types defined in CaTTS-DL, value constructors for time intervals and durations, arithmetic functions, and conditionals. CaTTS-CL's constraint symbols are common equation symbols, Allen's 13 interval relations [1], and the symbol ":" for type annotations. The complete syntax (of all CaTTS language fragments including CaTTS-CL) is given in Appendix A.

The constraint $X:\tau$ assigns to a variable X a finite domain over values of type τ (defined in CaTTS-DL). Note that the function symbols provided with CaTTS-CL are essentially the same as those provided with CaTTS-DL. Furthermore, the constraint symbols provided with CaTTS-CL have the same names as the predicate symbols provided with CaTTS-DL because type defining predicates and constraints are both boolean functions. However, there is an elementary difference between a CaTTS-CL constraint and a CaTTS-DL predicate: a constraint specifies the properties and relationships among partially unknown "objects". All possible solutions satisfying the constraint are computed by the constraint solver. In contrast, a predicate specifies the condition(s) to be satisfied by the elements belonging to some predicate subtype. E.g. the type defining predicate "holiday" specifies the infinite set of all holidays, and the constraint "X:holiday" computes the (infinite) set of all holidays. Thus, the values satisfying any CaTTS-CL constraint are computed, whereas a predicate only specifies the infinite set of values of some CaTTS-DL predicate subtype without performing any computations.

A CaTTS-CL program is a finite collection of CaTTS-CL constraints. Calendars defined in CaTTS-TDL are referred to by the use_calendar construct, data formats defined in CaTTS-FDL are referred to by the use_format construct, and external libraries are referred to by the import construct. The constraints specified in a CaTTS-CL program are delimited by the reserved words prog and end.

5.1 Use Case (Continued): Multi-Calendar Appointment Scheduling

Turning attention back to the two business men scheduling a phone conference (cf. Section 4.5) during the 1st week in October 2004, they specify the necessary constraints in a CaTTS-DL program (cf. Figure 7). The day, the phone conference might take place should be a Monday, Tuesday, Wednesday, or Thursday in Tel Aviv. The conference itself (denoted by the variable **Conf**) has a maximal duration of 1 hour, and it should be between 9 a.m. and 5 p.m. considering both time zones involved in this scenario. Furthermore, the telephone conference should take place in the first week of October 2004.

6. STATIC TYPE CHECKING AND CON-STRAINT REASONING SUMMARIZED

This section briefly summarizes the characteristics of CaT-TS' language processors. A *static type checker* to ensure the behavior and semantics of calendric data and constraints, and a *constraint solver* to reason with such data.

6.1 Static Type Checker

In programming languages such as ML [9] static type

checking is used as a "lightweight formal method" (i.e. merely syntactically tractable) for program analyses ensuring correct behavior of programs and/or systems w.r.t. some specification. CaTTS, however, uses static type checking for *semantic restrictions* of inherent ambiguous and/or imprecise calendric data and constraints ensuring correct interpretation of CaTTS-CL programs w.r.t. some CaTTS-DL calendar specification.

For space reasons, the typing and subtyping relations of CaTTS' static type checker cannot be presented in this article. First experimental results with a prototype implementation of CaTTS' type checker point to a good efficiency (i.e. type checking is polynomial). Further investigations concerning efficiency as well as soundness and completeness results are undergo.

6.2 Constraint Solver

CaTTS' constraint solver essentially works on arbitrary finite domains with type annotations after calendars defined in CaTTS-DL. It departs from constraint systems over finite domains [6] due to (i) typed constraint variables, and (ii) constraint variables that may range either over single values or over intervals of values; thus, reasoning over (possibly periodic) intervals. The constraint solver refers to and relies on the type predicates generated from a calendar definition in CaTTS-DL. This makes search space restrictions possible, and furthermore, obtains the semantics of calendric data and constraints introduced with CaTTS-DL type definitions.

7. RELATED WORK

CaTTS complements data type definition languages and data modeling and reasoning methods for the Semantic such as XML Schema [12], RDF [15], and OWL [14]: XML Schema provides a considerably large set of predefined time and date data types dedicated to the Gregorian calendar whereas CaTTS enables user-defined data types dedicated to any calendar. RDF and OWL are designed for *generic* Semantic Web applications. In contrast, CaTTS provides with methods *specific* to particular application domains, that of calendars and time.

CaTTS departs from time ontologies such as the KIF time ontology [8], the DAML time ontology [4], and time in OWL-S [10] in many aspects.

CaTTS considerably simplifies the modeling of specificities of cultural calendars (such as leap years, sun-based cycles like Gregorian years, or lunar-based cycles like Hebrew months) as well as the modeling of professional calendars often involving "gaps" in time (e.g. "working day"), "gapped" data items (e.g. data items of type "working week"), and periodic events (e.g. "CS123 lecture") due to predicate subtypes.

The well-known advantages of statically typed languages such as error detecting, language safety, efficiency, abstraction, and documentation whereas the two latter obtain particular interest due to overloaded semantics of calendric data apply to CaTTS, as well. Beyond this, CaTTS' static type checker provides both meta-type checking of predicate subtype definitions in CaTTS-DL and type checking of constraints in CaTTS-CL, obtaining the semantics of different time granularities even for reasoning with their granules.

CaTTS comes along with a constraint solver dedicated to calendar definitions in CaTTS-DL; this dedication makes considerable search space restrictions, hence gains in effi-

```
program TelConference =
use_calendar unqualified Gregorian;
use_calendar Hebrew, CET(C), EET(C);
use_format unqualified ISO.Extended;
prog
Conf:hour during X:week && X during "2004-10" && relative index X in october == 1 &&
relative index Conf in CET(Gregorian).day >= 9 &&
relative index Conf in CET(Gregorian).day <= 17 &&
relative index Conf in EET(Gregorian).day >= 9 &&
relative index Conf in EET(Gregorian).day <= 17 &&
conf during EET(Gregorian).day <= 17 &&
conf during EET(Gregorian).(monday|tuesday|wednesday|thursday)
end</pre>
```

Figure 7: A scheduling problem in CaTTS-CL.

ciency, possible.

While (time) ontologies follow the (automated reasoning) approach of "axiomatic reasoning", CaTTS is based on a (specific) form of "theory reasoning", an approach well-known through paramodulation. Like paramodulation ensures efficient processing of equality in resolution theorem proving, CaTTS provides the user with convenient constructs for calendric types and efficient processing of data and constraints over those types.

CaTTS inherently differs from specification languages for events and temporal expressions in natural language text such as TimeML [7]. TimeML is a language for annotating temporal information in text corpora whereas CaTTS is designed as a statically typed language specialized in calendar and time modeling and reasoning, addressed to Semantic Web applications and Web Services.

8. CONCLUSIONS

This article has introduced CaTTS, consisting of

- CaTTS-DL, a definition language, itself consisting of
 - CaTTS-TDL, a type definition language and
 - CaTTS-FDL, a date format definition language
- CaTTS-CL, a constraint language typed by CaTTS-DL definitions.

CaTTS' predicate subtype constructors allow for defining arbitrary time granularities as types in CaTTS-DL. The two subtype relations aggregation subtype of and inclusion subtype of provide means for conversions between those types during constraint reasoning with calendric data of those types, particularly in CaTTS-CL. CaTTS' polytypic constructors provide a convenient and intuitive manner to specify periodic events. Interpreting calendars as types and their parameterization ensures maintenance and reuse of calendars, where the "type" of a calendar provides a summary of that calendar.

CaTTS facilitates the modeling and efficient processing of calendar and time data in Web and Semantic Web applications and Web Services, especially compared to ontologybased modeling and reasoning.

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APPENDIX

A. SYNTAX OF CATTS

A.1 Identifiers

$t \in TyVar$	type	identifiers	long
$\mathbf{c} \in \mathbf{CalId}$	calendar	identifiers	long
$s \in CalSigId$	calendar signature	identifiers	
$f\in CalFunId$	calendar function	identifiers	
$\mathbf{p} \in \mathbf{ProgId}$	program	identifiers	

For each class of identifiers X marked "long" there is a class long X of long identifiers; if x ranges over X then long x

ranges over longX. The syntax of the long identifiers is given by the following:

:=			long identifiers:
	x		identifier
	c_1 .	 $.c_n.x$	qualified identifier $n \geq 1$

The long identifiers constitute a link between declarations and calendars.

A.2 Grammar

longx :

CaTTS grammar, including the syntactic forms for both language formalisms CaTTS-DL and CaTTS-CL is given in a BNF-like notation ($\langle \dots \rangle$ denote $n \leq 0$ repetitions).

e ::= exprs: k constantduration, $n \in \mathbb{N}$ n ty binOp e e binary op unOp e unary op alternate x:ty $\langle | e \rightarrow e \rangle$ alternateconstraintsce ce ::= constraints: х variable x:ty $domain\ constraint$ ce iRel ce interval relation ce aRel ce arithm. relation ce && ce conjunction binOp ::= shift forward | shift backward relative to | + | - | relative in | $* \mid \ \mid \ \texttt{mod} \mid \texttt{div} \mid$ max | min unOp ::= duration_of | begin_of | end_of | index equals | before | after | starts | started_by | finishes | finished_by | iRel ::= during | contains | meets | met_by | overlaps | overlapped_by aRel ::= == | <= | < | > | >= | != ty ::= types:type identifier longt reference reference refinement n @ e refine, $n \in \mathbb{N}$ aggregate e<,e>@ e aggregationselect x:ty where $e\langle e \rangle$ inclusion duration|ty| ty & ty & ty > conjunction $\begin{array}{c|c} ty & | ty \langle | ty \rangle \\ ty & \backslash ty \end{array}$ disjunctionexcept ty #< ty coarser-restrict ty #> ty finer-restrict dcl ::= decls: type t = ty typegroup t = wspec group dcl;dcl sequential wspec ::= with specs: with ty <type t where e;e for $t_1=t_2\rangle$ caldcl ::= calendar decls: declarationdc1 calendar calbind calendaremptycaldcl;caldcl sequentialcalbind ::= calendar binds: c<(:sige)>= cale cale ::= calendar exprs: generativecal caldcl end longc identifier f(cale) function application

<pre>fundcl ::=</pre>		fun decls:
	cal_fun funbind	generative
		empty
	fundcl;fundcl	sequential
<pre>funbind ::=</pre>		fun binding:
	f(c:s):s' = cale	<i>y y</i>
sigdcl ::=		s decls:
•	calendar type sigbind	generative
		empty
	sigdcl;sigdcl	sequential
sigbind ::=		s bindings:
•	s = sige	, , , , , , , , , , , , , , , , , , ,
sige ::=	6	s exprs:
0	sig spec end	generative
	s	identifier
spec ::=		specs:
1	type t <: ty	aggregation
	type t c : ty	inclusion
	group t c : tv	aroup
	calendar c:sige	calendar
	spec:spec	seauential
progdcl ::=		p decls:
1 0	се	constraint
	use_calendar(ungualified)	
	$longc_1 \dots longc_n$:	$n \ge 1$
	import (ungualified)	
	$lib_1 \dots lib_n$:	$n \ge 1$
	use format(ungualified)	
	cate1 caten :	$n \ge 1$
	program progbind	aenerative
	emntu	generative
	progdcl:progdcl	seguential
proghind ··=	progaci, progaci	n hinds.
brogering	D Droge	p otnuo.
proge ··=	b broge	n ernrs.
proge	prog progdel end	declaration
	n	identifier
	P	vacionijiei
catdcl ··=		cat decls.
	catalog cathind	aenerative
	format fid $ty = d$ where e	format
	101mao 11400, 4 more e	emntu
	catdcl:catdcl	sequential
cathind ··=	Sabasi, Sabasi	cat hinds.
caubina	$cd(\cdot s) = cate$	cut othus.
cate ··=		cat errors.
cat catdel end	aenerative	car capro.
sat outdor ond	cd	identifier
	cate.cd	aual id
	catalog cd	cataloa
	0	