

# *Automatic Guidance for Refinement based Formal Methods*

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- The rigour of formal methods brings a lot of benefits to the development of systems.
- However, it is still not widely used outside specific domains.
- A major problem is the need for expertise in:
  - Formal modelling.
  - Theorem proving.
  - Understanding the close relationship between proof and modelling.

**Goal: To abstract away from the complexities of proof obligations, providing high-level modelling guidance.**

Here, with a focus on refinement.

# Proof planning

Proof planning uses proof patterns to automate the search for proofs.

- Automatic proof failure analysis and patching.
- Reusability of proof strategies.

# Reasoned Modelling

An approach that provides high-level modelling guidance by combining proof and modelling patterns.

- Currently the ideas of reasoned modelling are being developed in Event-B.
- We are working in *Refinement Plans*, a type of reasoned modelling method that focus on refinement.

- A formalism that supports modelling and reasoning of discrete event systems.
- Uses a *posit-and-prove* style of modelling.
- Promotes the evolution of models through *refinement*.
- Uses mathematical proof to verify the consistency between refinement levels.

# Event-B Example: A logging system

Records whether a resource is allocated or unallocated.

Context
Sets <i>RESOURCES</i>
Machine
<b>Variables:</b> <i>resources</i> , <i>allocated</i> , <i>unallocated</i>
<b>Invariants:</b> $\text{resources} \in \mathbb{P}(\text{RESOURCES})$ $\text{allocated} \subseteq \text{resources}$ $\text{unallocated} \subseteq \text{resources}$ $\text{allocated} \cap \text{unallocated} = \emptyset$ $\text{allocated} \cup \text{unallocated} = \text{resources}$
Events ...
<b>Event</b> <i>unallocate</i> $\hat{=}$ <b>any</b> <i>r</i> <b>where</b> <i>r</i> $\in$ <i>allocated</i> <b>then</b> <i>allocated</i> $=$ <i>allocated</i> $\setminus \{r\}$ <i>unallocated</i> $=$ <i>unallocated</i> $\cup \{r\}$ <b>end</b>

# Refinement in Event-B

Handle the complexity of large systems through the use of abstraction.

Refinement in Event-B:

- Existing events can be split, merged or modified.
- New events can be added.
- Variables can be added and/or removed.
- Gluing invariants: relate the state of the abstract model with the state of the concrete model.

All refinement steps are verified through proof obligations.

# *Refinement Plans*

- Classify common patterns of refinement at the level of models.
- Combine modelling and proof knowledge.
- Detect partial matches of known patterns of refinement in a development.
- Provide user guidance in terms of modelling decisions.

- **Correcting refinements:** modifications to flawed refinements.
- **Layering refinements:** introduction of intermediate layers of abstraction in complex refinements.
- **Abstracting refinements:** reduction of the initial complexity of a development.
- **Suggesting refinements:** suggesting alternative refinement steps.
- **Increasing proof automation:** associated proof patterns.

**refinement plan = refinement method  
+ proof methods  
+ critics**

# *Refinement method*

- Describes a common pattern of refinement (abstract model, concrete model and gluing invariant).
- Represented with declarative preconditions.
- These preconditions identify partial or complete instances of the pattern within a user's refinement.

## Refinement method example: *sets-to-function*

An instance of this pattern requires the:

- abstract model to contain a partition of sets (many variables),
- concrete model to replace the partition with a function (one variable)

Abstract model	Concrete model
$state1 \subseteq Elements$ $state2 \subseteq Elements$ $state1 \cap state2 = \emptyset$ $state1 \cup state2 = Elements$	$Status = \{STATE1, STATE2\}$ $fStatus \in Elements \rightarrow Status$ $state1 = fStatus^{-1}[\{STATE1\}]$ $state2 = fStatus^{-1}[\{STATE2\}]$

# Proof methods<sup>1</sup>

- Reasoning patterns associated to a refinement method.
- Proof methods are used when a user's refinement fully matches with a pattern but it has a set of unproven POs.
- The use of proof methods and the analysis of partial success at the level of proof planning represents future work.

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<sup>1</sup>Taken from Computational Logic [Bundy, 1991]

- Exception handling mechanism.
- If a partial instance of a refinement method is found, critics are applied.
- Represented with declarative preconditions.
- All preconditions must succeed for a critic to be applicable.
- Modelling guidance to overcome the failure is automatically generated (e.g. change guard/action/(gluing) invariants).
- The decision of applying/choosing guidance is left to the user.

# Example: Logging system applied to the sets-to-function refinement method

Precondition: There must exists a set of gluing invariants with the pattern:  
**stateVariable** = **concreteFunction**<sup>-1</sup>[{**stateConstant**}]

Abstract model	Concrete model
$allocated \subseteq Resources$ $unallocated \subseteq Resources$ $unallocated \cap unallocated = \emptyset$ $unallocated \cup unallocated = Resources$	$Status = \{ALLOCATED, UNALLOCATED\}$ $rStatus \in Resources \rightarrow Status$  <i>Missing gluing invariants</i>

There exists a partial instance of the refinement method!

# Gluing\_Invariant\_Speculation critic – Key ideas

- 1 There exists a failed guard strengthening PO in the concrete model with the form:

$\exists \text{failed\_po} \in \{\langle \_, \_, \_, \text{PO} \rangle \in \text{POs} \mid \text{failed\_proof}(\text{PO})\}.$

$\text{failed\_po} = \langle M, E, \_ / \text{GRD}, (\Delta, \underbrace{\text{stateFunction}(x) = Y} \vdash \underbrace{x \in \{z\}}) \rangle$

*concrete guard*      *abstract guard*

- 2 That by adding the gluing invariant pattern to the set of hypotheses the failed PO is provable:

$\text{provable } (\Delta, \text{stateFunction}(x) = Y, \underbrace{\{z\} = \text{stateFunction}^{-1}[\{Y\}]} \vdash x \in \{z\})$

## Instantiation of the critic: logging example

- 1 Failed POs with the form “ $\Delta, stateFunction(x) = Y \vdash x \in \{z\}$ ”: ✓

$\dots, rStatus(r) = ALLOCATED \vdash r \in \{allocated\}$

$\dots, rStatus(r) = UNALLOCATED \vdash r \in \{unallocated\}$

- 2 The addition of the gluing invariant discharges the POs: ✓

*provable* ( $\dots, rStatus(r) = ALLOCATED,$

$\{allocated\} = rStatus^{-1}[\{ALLOCATED\}] \vdash r \in \{allocated\}$ )

(A similar instantiation is given for state unallocated)

All preconditions succeed, then the guidance is the addition of the gluing invariants in the concrete model.

# The REMO<sup>2</sup> tool

<sup>2</sup>The REMO acronym follows from REasoned MOdelling

# Ongoing and future work

- Development of more refinement plans and their evaluation through case studies.
- Explore the role of refinement plans for:
  - Guiding users in their initial choice of refinement.
  - Suggesting intermediate refinement steps.
- Tool implementation: *REMO*.
- Development of the proof planning mechanism to exploit proof methods.

# Conclusions

- Refinement plans aim at providing modelling guidance by automatically analysing specifications that lie just outside a known pattern of refinement.
- While the analysis of failure and generation of guidance is automatic, the decision as to whether or not to take the guidance on offer will be left to the user.
- We believe that this approach will enable us to turn low-level proof-failures into high-level modelling guidance.

# Refinement plan and critic schemas

PLAN( <i>Name</i> )	CRITIC( <i>Name</i> )
INPUTS:	INPUTS:
PO_SET { <i>POs</i> }	PO_SET { <i>POs</i> }
MODELS { <i>AM, CM</i> }	MODELS { <i>AM, CM</i> }
REFINEMENT METHOD:	R_INSTANCES { <i>Instances</i> }
1. <i>Precondition</i>	P_INSTANCES { <i>Instances</i> }
....	PRECONDITIONS:
I. <i>Precondition</i>	1. <i>Precondition</i>
PROOF METHODS:	....
1. <i>Proof_Method</i>	L. <i>Precondition</i>
....	OUTPUTS:
J. <i>Proof_Method</i>	PATCH <i>patch description</i>
CRITICS:	GUIDE <i>guidance description</i>
1. <i>Critic_Name</i>	
....	
K. <i>Critic_Name</i>	