

#### Parallel Programming in Erlang using Skel

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Basic course in Parallel Programming using Skeletons in Erlang

- 1. Introduction to "Skel"
- 2. Building patterns in Skel
  - 1. Seq
  - 2. Pipeline
  - 3. Farm
  - 4. Combining
- 3. Introducing granularity

By the end, you will be able to write parallel programs!

### The Skel Library for Erlang



- Skeletons implement specific parallel patterns
  - Pluggable templates
- Skel is a new (AND ONLY!) Skeleton library in Erlang
  - map, farm, reduce, pipeline, feedback
  - instantiated using **skel:do**
- Fully Nestable Skel.weebly.com
- A DSL for parallelism

https://github.com/ParaPhrase/skel

OutputItems = skel:do(Skeleton, InputItems).



#### www.skel.weebly.com

#### SKEL: A STREAMING PARALLEL SKELETON LIBRARY FOR ERLANG





#### Skel Overview



- Structured parallel programming framework
  - "palette" of skeletons/parallel patterns available (almost) arbitrary composition supported
  - very hard to implement arbitrary parallel schema
- Streaming parallel programming framework
  - primitive support to process streams of tasks

#### Skel. Who? Where?



- Main developers at St Andrews
  - Me <sup>(c)</sup>, Adam Barwell, Sam Elliott, Vladimir Janjic, Kevin Hammond, ...
- Used on EU projects, ParaPhrase (FP7; ended 2015)
- Contributions from Open-source community
  - Poland, Sheffield, Hungary, ...
- Used for all sorts of problems:
  - EMAS, image processing, GPU programming,
- Code available on git: https://github.com/ParaPhrase/skel

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#### skel

A Streaming Process-based Skeleton Library for Erlang

#### Usage

make to compile the library source

#### Skeletons supported



- Stream parallel
  - Pipeline (computations in stages)
  - Farm (Embarassingly parallel...)
  - Feedback loop (route back output tasks satisfying condition)
- Data parallel
  - Map (applying function over all items in stream)
  - Reduce ("summing" up items in a stream)
- Non primitive
  - Divide and conquer
  - Stencil
  - ...



### The Concept of Parallelism



- Input queue
  - Feeds tasks from an input stream
  - Connected to the 'parallel activity'
- Parallel activity body
  - Processes each item appearing onto the input stream
  - Delivers a result to the output stream
  - Maybe sequential *or* parallel
- Output queue
  - Receives output results from parallel body
  - Possibly connected to the input of another parallel activity
  - May not preserve order

#### Loading skel



- \$ cd skel
- \$ make examples
- \$ make console



#### Wrapping things up: the Seq skeleton

• Used to wrap up a function



% → [2,3,4,5,6,7,8,9,10,11]

#### Parallel Pipeline Skeleton



- Each stage of the pipeline can be executed in parallel
- The input and output are streams



skel:do([{pipe,[Skel1, Skel2,...,SkelN]}], Inputs).

#### Pipeline – 1<sup>st</sup> example





```
> cd skel
> make console
erl> skel:do(
   [{pipe,
      [{seq, fun(X) -> X+1 end}]}], [1,2,3,4,5]).
```

#### Pipeline – 2nd example





```
> cd skel
> make console
erl> skel:do(
   [{pipe,
      [{seq, fun(X) -> X+1 end},
      {seq, fun(Y) -> Y+1 end}]}],
      [1,2,3,4,5]).
```



#### **Constructing Pipeline Workers**

- > Stage1 = {seq, fun(X) ->
   {fib:fib(X), X} end}.

#### Using a pipeline



- > InputsP = lists:duplicate(8, 27).
- > {T2P, V2P} = timer:tc(fun() ->
   skel:do([{pipe,
   [Stage1,Stage2]}],
   InputsP) end).



#### Creating a sequential pipeline

> Stage1S = fun(X) -> {fib:fib(X), X}
end.

> Stage2S = fun({X,Y}) -> fib:fib(Y)
end.

```
> {T1P, V1P} = timer:tc(fun() ->
  [ Stage2S(Stage1S(X)) || X <- InputsP
] end).</pre>
```

> T1P / T2P.

#### Farm Skeleton



- Each worker is executed in parallel
- A bit like a 1-stage pipeline



skel:do([{farm, Skel, M}], Inputs).

![](_page_18_Figure_0.jpeg)

> cd skel
> make console
erl> skel:do([{farm, [fun(X) -> X+1 end], 2}], [1,2,3,4,5]).

#### Using a Farm

![](_page_19_Picture_1.jpeg)

> Payload = {seq, fun(X) ->
fib:fib(X) end}.

> Inputs = lists:duplicate(8, 27).

> NumberWorkers = 4.

> skel:do([{farm, [Payload], NumberWorkers}], Inputs).

#### Timing the farm

![](_page_20_Picture_1.jpeg)

> T1 / T2.

![](_page_21_Picture_0.jpeg)

## Matrix Multiplication

![](_page_22_Figure_0.jpeg)

https://en.wikipedia.org/wiki/Matrix\_multiplication#/media/File:Matrix\_multiplication\_diagram\_2.svg

![](_page_23_Picture_0.jpeg)

#### Sequential Implementation

```
main(Nrows, S) ->
MatrixA = randmat(Nrows, Nrows, S),
MatrixB = randmat(Nrows, Nrows, S),
productMat(MatrixA, MatrixB).
```

```
productMat(MatrixA, MatrixB) ->
    mult(rows(MatrixA), cols(MatrixB)).
```

```
mult([],_) -> [];
mult([R|Rows], Cols) ->
    [lists:map(fun(X) ->
        multSum(R, X) end, Cols)
        | mult(Rows, Cols)].
```

```
multSum(R, C) ->
    lists:sum([A*B || {A,B} <- lists:zip(R,C) ] ) .</pre>
```

#### Naïve parallelisation

![](_page_24_Picture_1.jpeg)

mult\_par\_2([],\_) -> []; mult\_par\_2([R|Rows], Cols) -> [skel:do([{farm, [{seq, fun(C) -> multSum(R,C) end}],10}], Cols) | mult(Rows, Cols)].

#### Better parallelisation

![](_page_25_Picture_1.jpeg)

![](_page_26_Picture_0.jpeg)

```
multSum_par_1(R,C) ->
    lists:sum(skel:do([{farm, [{seq, fun({A,B}) -> A*B
end}],10}], lists:zip(R,C))).
```

![](_page_27_Picture_0.jpeg)

```
multSum_par_2(R,C) ->
    skel:do([{reduce, fun(A, B) -> A*B end, fun id/1}],
lists:zip(R,C)).
```

#### Image Processing Example

![](_page_28_Picture_1.jpeg)

![](_page_28_Figure_2.jpeg)

Write Image

#### **Basic Erlang Structure**

![](_page_29_Picture_1.jpeg)

```
readImage({In1, in2, out) ->
```

```
{ Image1, Image2, out}.
```

```
convertImage({Image1, Image2, out}) ->
   Image1P = whiteScreen(Image1),
   Image2P = mergeImages(Image1, Image2),
   {Image2P, out}.
```

```
writeImage({Image, Out}) -> ...
```

#### Map Skeleton

![](_page_30_Picture_1.jpeg)

![](_page_30_Figure_2.jpeg)

skel:do([{map, Skel, Decomp, Recomp}], Inputs).

![](_page_31_Picture_0.jpeg)

#### Introduce Map

{seq, Expr}

### {map, {seq, Expr'}, fun ?MODULE:split/1, fun ?MODULE:recomp/1}

Expr', split and recomp are arguments to the refactoring

#### **Cluster Skeleton**

![](_page_32_Picture_1.jpeg)

![](_page_32_Figure_2.jpeg)

#### Using The Right Pattern Matters

![](_page_33_Picture_1.jpeg)

#### Speedups for Matrix Multiplication

![](_page_33_Figure_3.jpeg)

#### Cost Models

![](_page_34_Picture_1.jpeg)

$$T_{C_{pipeline}}(L) = max_{i=1..m}(T_{stage_i}(L)) + T_{copy}(L)$$

$$\begin{split} T_{C_{map}}(L) &= T_{distrib}(N_w,L) + \frac{T_{Fun}(L)}{Min(N_p,N_w)} + T_{gather}(N_w,L) \\ & \text{where } N_W = npartitions(L) \end{split}$$

$$T_{C_{farm}}(N_w, L) = max\{T_{emitter}(N_{p,N_w}, L), \frac{T_{Fun}(L)}{Min(N_p, N_w)}, T_{collector}(N_w, L)\}$$
(2)

#### Case Study: De-Noising

![](_page_35_Picture_1.jpeg)

![](_page_35_Picture_2.jpeg)

Original Baboon standard test image 1024x1024

36

#### Restored

![](_page_35_Picture_5.jpeg)

PNSR 43.29dB MAE 0.35

PNSR 32.75dB MAE 2.67

90% impulsive noise

![](_page_35_Picture_9.jpeg)

PNSR 23.4 MAE 11.21

![](_page_36_Picture_0.jpeg)

denoise(Ims) -> [ filter (geoRef ( Im ) ) || Im <- Ims ].</pre>

![](_page_36_Figure_3.jpeg)

![](_page_37_Picture_0.jpeg)

#### Stage 1: Introduce Par Map

(Max(171, 466) \* 1024) 477184

(Max(171, (0.001 + 29 + 0.001)) \* 1024)

175104

![](_page_38_Picture_0.jpeg)

#### Stage 1: Introduce Task Farm

```
denoise(Ims) -> skel:run([{pipe, [{seq, fun ?MODULE:geoRef/1},
                        {parmap, [{seq,fun ?MODULE:filter'/1}],
                                 fun ?MODULE:partition/1,
                                 fun ?MODULE:combine/1}]}, Ims).
denoise(Ims) -> skel:run([{pipe,[{farm,[{seq,fun ?MODULE:geoRef}],
                    Nw}, {parmap, [{seq, fun ?MODULE:filter'}],
                              fun ?MODULE:partition/1,
                              fun ?MODULE:combine/1}]}, Ims).
     (Max(171, (0.001 + 29+ 0.001)) * 1024)
                                                   175104
```

(Max(171/8, (0.001 + 29+ 0.001)) \* 1024)

29698

#### **Performance Results**

![](_page_39_Picture_1.jpeg)

- 8 Core Dell PowerEdge
  - 24 Core Dual AMD Opteron 6176 2.3GHz
  - 12GB RAM
  - 6MB L2 Cache
  - Linux 2.6.18
  - Erlang 5.9.1 R15
- Runtimes averaged over 10 runs
- Input of 1024 images

# Predicted vs. Actual Speedups for Erlang

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Speedups for denoise

![](_page_40_Figure_2.jpeg)

![](_page_41_Picture_0.jpeg)

# Thank you!

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