Does Individual Behavior Matter? Network and Homogenous Models



Shweta Bansal and Lauren Ancel Meyers University of Texas, Austin

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Traditional Compartmental Models



$$\frac{dS}{dt} = -\lambda S$$
$$\frac{dI}{dt} = \lambda S - \gamma I$$
$$\frac{dR}{dt} = \gamma I$$

Network Interpretation of Compartmental Model I

Complete Graph- possible contacts





Network Interpretation of Compartmental Models II

Force of Infection



Regular Random Graph – *effective contacts*



What are the structures of real networks?



How to incorporate heterogeneity?

Network & Individual-Based Models

- Percolation methods
 (Newman et al, 2000, 2002; Meyers et al, 2003, 2005, 2006)
- Pair approximation methods (Keeling 1999)
- Heterogeneous-mixing methods (Moreno, Pastor-Satorras, Vespignani, 2002)
- Dynamical PGF methods (Volz, 2007)

How to incorporate heterogeneity?

Modified Compartmental Models

$$\frac{dS}{dt} = -\lambda S = -\alpha \tau (I/N) S$$

Aparicio & Pascual (2006): $\frac{dS}{dt} = -\gamma R_0 (I/N) S$

Roy & Pascual (2006), Severo (1969), Hochberg (1991), Liu et al (1987), Stroud et al (2006)

$$\frac{dS}{dt} = -\alpha \tau \left(I/N \right)^p S^q$$

What is the correct modifier?

$$\frac{dS}{dt} = -\lambda S = -\alpha \tau (I/N) S$$



What is the correct modifier?



Modified Force of Infection



Conclusions

• What have simpler models been missing, if anything?

• Which models should we use in the future?

Ref: Bansal, Grenfell, Meyers. J. R. Soc. Interface (2007)