

F28PL1 Programming Languages

Lecture 12: Standard ML 2

Declaration

introduce a variable

associate identifier with value

- *val identifier = expression;*

> *val identifier = value : type*

identifier - any sequence of letters,
digits and _

starting with a letter

use *identifier* in subsequent
expressions to return *value*

Declaration

```
- val toPound = 0.66;  
> val toPound = 0.66 : real  
  
- 27.45*toPound;  
> 18.117 : real  
  
- val employee =  
  ("Duncan", "Thaw", 19000.0);  
> val employee =                ("Duncan", "Thaw", 19000.0) :  
                                string * string * real  
  
- val payPounds = #3 employee*toPound;  
> val payPounds = 12540.0 : real
```

Declaration

can't assign new value to declared variable

can *redeclare* variable by entering new definition

```
- val toPound = 0.68;
```

```
> val toPound = 0.68 : real
```

creates a *new instance* of the variable

does not assign to existing variable

Function

function

mapping from a *domain* to a *range*

domain - formal parameters

range - result

function type displayed as

fn : domain type -> range type

Function

can display types of prefix system functions

```
- size;
```

```
> fn : string -> int
```

i.e. size takes a string and returns an int

```
- not;
```

```
> fn : bool -> bool
```

i.e. not takes a bool and returns an int

Function definition

```
fun identifier pattern = expression;
```

identifier

name associated with function

pattern

formal parameters

to begin with, an *identifier*

expression

function *body*

Function definition

system shows function type

can't display function value

```
- fun ident pattern = expression;
```

```
> val ident = fn : type1 -> type2
```

type1 - type for *pattern* - domain

type2 - type for *expression* - range

Function definition

system uses *polymorphic type checking* to deduce types from use of operators/values of known type

e.g. increment an integer

```
- fun inc x = x+1;
```

```
> val inc = fn : int -> int
```

```
1 is int so ...
```

```
+ must be int addition so...
```

- x must be int

Function definition

e.g. put "s" on end of a string

```
- fun plural w = w^"s";
```

```
> val plural = fn : string -> string
```

^ takes 2 strings so...

w must be string

^ returns a string so...

w must be string and "s" must be string

Function definition

e.g. given string, return it with its length

```
- fun sSize s = (s, size s);
```

```
> val sSize =
```

```
    fn : string -> string * int
```

size takes a string so...

s must be string

size returns int

Explicit formal parameter types

sometimes can't deduce type in presence of overloaded operators

e.g. square an integer

```
fun sq x = x*x
```

can't tell if * is int or real

use *explicitly typed* pattern: *(pattern:type)*

```
- fun sq (x:int) = x*x;
```

```
> val sq = fn : int -> int
```

Function call

must call a *type1* -> *type2* function with a *type1* actual parameter to return a *type2* result

- *ident expression1*;

> *value2* : *type2*

system:

1. evaluates *expression1* to give *value1* of type *type1*
2. finds *type1* -> *type2* function associated with *ident*
3. replaces's *idents* formal parameter with *value1* in *idents* body
4. evaluates *idents* body to return *value2* of *type2*

Function call

substitution model of function call

- `inc 3;`

> `4 : int`

`inc 3 ==> 3+1 ==> 4`

- `plural "banana";`

> `"bananas" : string`

`plural "banana" ==>`

`"banana" ^ "s" ==>`

`"bananas"`

Function call

```
- sSize "fish";  
> ("fish",4) : string * int  
sSize "fish" ==>  
("fish",size "fish") ==>  
("fish",4)  
- sq 7;  
> 49 : int  
sq 7 ==> 7*7 ==> 49
```

Multiple arguments

```
fun ident patt1 patt2 ... pattN =  
exp;
```

if:

```
patt1 : type1 ... pattN : typeN
```

```
exp : typeN+1
```

then function type is:

```
type1 -> ... -> typeN -> typeN+1
```


Multiple arguments

e.g. sum of squares

```
- fun sumsq x y = sq x + sq y;
```

```
> val sumsq = fn : int -> int -> int
```

sq is `int -> int` so...

x must be `int`

sq is `int -> int` so...

y must be `int`

sq x is `int` and sq y is `int` so...

+ must be `int` addition

Multiple arguments

```
- sumsq 3 4;
```

```
> 25 : int
```

```
sumsq 3 4 ==>
```

```
sq 3+sq 4 ==>
```

```
9+16 ==>
```

```
25
```

Multiple arguments

e.g. does a string have more than n letters?

```
- fun isMore s n = size s > n;
```

```
> val isMore : fn string -> int -> bool
```

size takes a string so...

```
  s is string
```

size s returns an int so...

```
> is int comparison so...
```

- n is int

```
> returns a bool
```

Multiple arguments

```
isMore "hello" 6;
```

```
> false : bool
```

```
ismore "hello" 6 ==>
```

```
size "hello" > 6 ==>
```

```
5 > 6 ==>
```

```
false
```

Multiple cases

can define functions with multiple cases

```
fun ident patterns1 = expression1 |  
    ident patterns2 = expression2 |  
    ...
```

patterns is one or more *pattern*

pattern may be

constant

identifier

patterns must be of same types

expressions must be of same type

Multiple cases

for function call:

actual parameters matched against each *patterns* in turn

when all match succeeds, value of corresponding *expression* returned

match:

constant - must be same as actual parameter value

identifier - *identifier* in body *expression* replaced with actual parameter

should have a case for all possible combinations of *patterns* values

Multiple cases

e.g. is integer 0?

```
- fun isZero 0 = true |  
  isZero x = false;
```

```
> val isZero = fn : int -> bool
```

0 is int so...

x must be int

true and false both bool so...

result is bool

Multiple cases

```
- fun isZero 0 = true |  
    isZero x = false;  
  
> val isZero = fn : int -> bool  
  
- isZero 0;  
  
> true : bool  
  
0 matches 0 ==> true  
  
- isZero 3;  
  
> false : bool  
  
3 doesn't match 0  
  
3 matches x ==> false
```


Multiple cases

e.g. rainbow colour sequence

```
- fun next "red" = "orange" |  
  next "orange" = "yellow" |  
  next "yellow" = "green" |  
  next "green" = "blue" |  
  next "blue" = "indigo" |  
  next "indigo" = "violet" |  
  next s = s^": not a valid colour";  
  
> val next = fn : string -> string  
"red", "orange" ... all string so s must be string  
all results are string
```

Multiple cases

```
- next "blue";
```

```
> "indigo" : string
```

```
"blue" doesn't match "red"
```

```
"blue" doesn't match "orange"
```

```
...
```

```
"blue" matches "blue" ==> "indigo"
```

Multiple cases

```
- next "banana";
```

```
> "banana not a valid colour" : string
```

```
"banana" doesn't match "red"
```

```
...
```

```
"banana" matches s ==>
```

```
"banana" ^ " not a valid colour" ==>
```

```
"banana: not a valid colour"
```

Wildcard pattern

`_` - matches anything and ignores it

e.g. don't use `x` on right hand side of 2nd case of `isZero`

```
- fun isZero 0 = true |  
    isZero _ = false;
```

```
> val isZero = fn : int -> bool
```

```
- isZero 22;
```

```
> false : bool
```

22 doesn't match 0

22 matches `_` ==> false

Non-sequential conjunction

```
- fun  AND false false = false |
      AND false true  = false |
      AND true  false = false |
      AND true  true  = true;

> val AND = fn : bool -> bool -> bool

- AND true false;

> false : bool

true false doesn't match false false
true false doesn't match false true
true false matches true false ==> false
```

Non-sequential conjunction

if 1st actual parameter is false then result is false

if 1st actual parameter is true then result is same as second actual parameter

simplify:

```
- fun AND false _ = false |
```

```
  AND true y = y;
```

```
> val it AND = fn : bool -> bool -> bool
```

Recursion 1

recursion is functional programming equivalent of iteration in imperative language

usually recurse across a range

base case

at end of range

function returns a value

recursion case

function combines result of processing next in range with result of processing rest of range

i.e. recursion case makes progress towards base case

Recursion 1

for integers, range is often from some positive value,
say n , to 0

base case: $n=0 \implies$ return value

recursion case: $n>0 \implies$ process n and
recurse with $n-1$

e.g. sum integers from 0 to n

base case: $n=0 \implies$ sum is 0

recursion case: $n>0 \implies$

add n to summing from 0 to $n-1$

Recursion 1: integer

- fun sum 0 = 0 |

 sum n = n+sum (n-1);

> val sum = fn : int -> int

0 is int so n must be int

0 is int so ...

 n+sum (n-1) must be int so ...

 + must be int addition so ...

 n must be int (!) and sum (n-1) must be
int

Recursion 1: integer

- sum 3;

> 6 : int

sum 3 ==>

3+sum 2 ==>

3+(2+sum 1) ==>

3 + (2+(1+sum 0)) ==>

3+(2+(1+0)) ==>

6

Recursion 1: integer

e.g. find 2 to the power n

base case: $n=0 \implies 1$

recursion case: $n>0 \implies$ multiply 2 by 2^{n-1}

```
- fun pow2 0 = 1 |
```

```
    pow2 n = 2*pow2 (n-1);
```

```
> val pow2 = fn : int -> int
```

0 is int so n must be int

0 is int so * must be int multiplication so

2 must be int and pow2 (n-1) must be int

Recursion 1: integer

- pow2 3;

> 8 : int

pow2 3 ==>

2*pow2 2 ==>

2*(2*pow2 1) ==>

2*(2*(2*pow2 0)) ==>

2*(2*(2*1)) ==> 8

Recursion 1: integer

e.g. find x to the power n

base case: $n=0 \implies 1$

recursion case: $n>0 \implies$ multiply x by x^{n-1}

```
- fun power _ 0 = 1 |
```

```
    power x n = x*power x (n-1);
```

```
> val power = fn : int -> int -> int
```

1 is int so $x \cdot \text{power } x \text{ (n-1)}$ must be int so $*$
must be int multiplication so x must be int

0 is int so n must be int

Recursion 1: integer

- power 3 3;

> 27 : in

power 3 3 ==>

3*power 3 2 ==>

3*(3*power 3 1) ==>

3*(3*(3*power 3 0)) ==>

3*(3*(3*1)) ==> 27

Recursion 1

e.g. make a string with n "."s

base case: $n=0 \implies ""$

recursion case: $n>0 \implies$ join "." to $n-1$ "."s

- fun stops 0 = "" |

stops n = "."^stops (n-1);

> val stops = fn : int -> string

0 is int so n must be int

"" is string so "."^stops (n-1) must be string
so ^ must return string (!) so "." must be
string (!) so stops (n-1) must be string

Recursion 1: integer

```
- stops 3;
```

```
> "...": string
```

```
stops 3 ==>
```

```
"."^stops 2 ==>
```

```
"."^("."^stops 1) ==>
```

```
"."^("."^("."^stops 0)) ==>
```

```
"."^("."^("."^"")) ==>
```

```
"..."
```


Recursion 1: integer

e.g. make a string with `n` lots of string `s`

base case: `n=0 ==> ""`

recursion case: `n>0 ==> join s to n-1 s's`

```
- fun sJoin _ 0 = "" |  
    sJoin s n = s^sJoin s (n-1);  
> val sJoin =  
    fn : string -> int -> string
```

Recursion 1: integer

```
- sJoin 3 "run";
```

```
> "runrunrun" : int
```

```
sJoin 3 "run" ==>
```

```
"run" ^ sJoin 2 "run" ==>
```

```
"run" ^ ("run" ^ sJoin 1 "run") ==>
```

```
"run" ^ ("run" ^ ("run" ^ sJoin 0 "run")) ==>
```

```
"run" ^ ("run" ^ ("run" ^ "")) ==>
```

```
"runrunrun"
```

Partial application 1

apply a function of n formal parameters to $m < n-1$ actual parameters

forms a new function of $n-m$ formal parameters

like original function

with formal parameters $1..m$ *frozen* to actual parameters $1..m$

Partial application 1

```
- fun f a b c d = ...
```

```
> val f =
```

```
    fn : type1 -> type2 -> ... typeN
```

```
- val aval = ...;
```

```
> val aval = ...: type1
```

```
- val f' = f aval;
```

```
> val f' : type2 -> ... typeN
```

f' is like *f* with *a* frozen to the value of *aval*

Partial application 1

e.g. powers

```
- fun power _ 0 = 1 |
```

```
    power x n = x*power x (n-1);
```

```
> val power = fn : int -> int -> int
```

```
- val pow2 = power 2;
```

```
> val pow2 = fn : int -> int
```

pow2 is like power with x frozen to 2

```
- pow2 3;
```

```
> 8 : int
```

```
pow2 3 ==> power 2 3 ==> ... 8
```

Partial application 1

e.g. sJoin

```
- fun sJoin _ 0 = "" |
    sJoin s n = s^sJoin s (n-1);
> val sJoin = fn : string -> int -> string
- val stops = sJoin ".";
> val stops = fn : int -> string
stops is like sJoin with s frozen to "."
- stops 3;
> "...": string
stops 3 ==> sJoin "." 3 ==> ... "..."
```

Conditional expression

pattern matching with constant can detect presence or absence of value

can't check properties of value

conditional expression

if expression1

then expression2

else expression3

expression1 must return bool

expression2 and *expression3* must return same type

Conditional expression

e.g. find absolute value of integer

```
- fun abs x =
```

```
    if x >= 0
```

```
    then x
```

```
    else ~x;
```

```
> val abs = fn : int -> int
```


Conditional expression

e.g. find bigger of two integers

```
- fun max (x:int) y =  
    if x>y  
    then x  
    else y;
```

```
> val max = fn : int -> int -> int
```

NB > is overloaded so must make type of one of x or y explicit