Using Mathematics and History to Predict the Future of Semi-Arid Vegetation

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This talk can be downloaded from my web site

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In this talk I will discuss the use of mathematical models to:

- predict future vegetation levels in semi-arid regions
- infer the historical origin of vegetation in semi-arid regions

Outline



Vegetation Pattern Formation

- 2 History-Dependence in Vegetation Patterns
- 3 Global Climate Models and Historical Climate Data
- Predicting Future Vegetation Levels
- 5 Inferring the Historical Origin of Patterned Vegetation

Vegetation Pattern Formation

History-Dependence in Vegetation Patterns Global Climate Models and Historical Climate Data Predicting Future Vegetation Levels Inferring the Historical Origin of Patterned Vegetation



Vegetation Patterns Banded Vegetation on Slopes

Vegetation Pattern Formation

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Vegetation Patterns

Vegetation Patterns Banded Vegetation on Slopes

Desert ecosystems provide a classic example of self-organised pattern formation.



W National Park, Niger Average patch width is 50 m

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Predicting the Future of Semi-Arid Vegetation

Vegetation Patterns Banded Vegetation on Slopes

Vegetation Patterns

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Data from Burkina Faso Rietkerk et al Plant Ecology 148: 207-224, 2000

 $\begin{array}{l} \mbox{More plants} \Rightarrow \mbox{more roots and organic matter in soil} \\ \Rightarrow \mbox{more infiltration of rainwater} \end{array}$

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Predicting the Future of Semi-Arid Vegetation

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Banded Vegetation on Slopes

On slopes, run-off occurs in one direction only, giving striped patterns parallel to the contours.



Bushy vegetation in Niger



Mitchell grass in Australia (Western New South Wales)

Banded vegetation patterns are found on gentle slopes in semi-arid areas of Africa, Australia, Mexico and S-W USA.

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Predicting the Future of Semi-Arid Vegetation



Mathematical Model of Klausmeier Typical Solution of the Model Variations in Rainfall: Hysteresis



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Mathematical Model of Klausmeier Typical Solution of the Model Variations in Rainfall: Hysteresis

Mathematical Model of Klausmeier



(Klausmeier, Science 284: 1826-8, 1999)

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Mathematical Model of Klausmeier



The nonlinearity in water uptake occurs because the presence of plants increases water infiltration into the soil.

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Typical Solution of the Model



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Pattern Existence and Stability

High rainfall \Rightarrow uniform vegetation Low rainfall \Rightarrow no vegetation Medium rainfall \Rightarrow patterns



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Pattern Stability: The Key Result

Key Result

Many of the possible patterns are unstable and thus will never be seen.

However, for a wide range of rainfall levels, there are multiple stable patterns.

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www.ma.hw.ac.uk/~jas Predicting the Future of Semi-Arid Vegetation

Variations in Rainfall: Hysteresis

Variations in Rainfall: Hysteresis

Model prediction: as rainfall is varied within the range giving patterns, abrupt changes in pattern wavelength occur.





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Variations in Rainfall: Hysteresis

Wavelength changes abruptly at the edge of the Busse Balloon.



Rainfall

(work of JAS, Koen Siteur, Eric Siero, Arjen Doelman, Max Rietkerk)

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Global Climate Models Approaches to Predicting Future Vegetation Rainfall Predictions for the Sahel Rainfall History in the Sahel Historical Rainfall Data Set

- 1) Vegetation Pattern Formation
- History-Dependence in Vegetation Patterns
- Global Climate Models and Historical Climate Data
- Predicting Future Vegetation Levels
- Inferring the Historical Origin of Patterned Vegetation



Global Climate Models Approaches to Predicting Future Vegetation Rainfall Predictions for the Sahel Rainfall History in the Sahel Historical Rainfall Data Set



Question: How will vegetation levels in the Sahel region of Africa change over the remainder of the century?

Global Climate Models

Global Climate Models Approaches to Predicting Future Vegetation

- Prediction of future climate is an active research area: 60 models in CMIP5, results of CMIP6 due in 2020
- Some of these models include "dynamic vegetation" (12/60 in CMIP5)
- But: spatial grid cells (~100km) are too large to deal effectively with patterned vegetation
- This is demonstrated by the huge variability in predictions of future vegetation levels in the Sahel.



So: a different approach is needed

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Global Climate Models Approaches to Predicting Future Vegetation Rainfall Predictions for the Sahel Rainfall History in the Sahel Historical Rainfall Data Set

Approaches to Predicting Future Vegetation

- Improve the spatial resolution in global climate models: in progress but a resolution suitable for patterned vegetation lies well in the future.
- Improve models for patterned vegetation, to include some climate data or feedbacks (e.g. work of Mara Baudena & Max Rietkerk)

My approach: use predictions of future rainfall from global climate models (CMIP5) as a forcing term in a simple model for semi-arid vegetation.

 Vegetation Pattern Formation
 Global Climate Models

 History-Dependence in Vegetation Patterns
 Approaches to Predicting Future Vegetation

 Global Climate Models and Historical Climate Data
 Predicting Future Vegetation Levels

 Predicting Future Vegetation Levels
 Rainfall History in the Sahel

 Inferring the Historical Origin of Patterned Vegetation
 Historical Rainfall Data Set

Rainfall Predictions for the Sahel

Predictions of future rainfall for the Sahel are highly variable.



In view of this, is it possible to make meaningful predictions of future vegetation?

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Predicting the Future of Semi-Arid Vegetation

 Vegetation Pattern Formation
 Global Climate Models

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Rainfall Predictions for the Sahel

Predictions of future rainfall for the Sahel are highly variable.



- In view of this, is it possible to make meaningful predictions of future vegetation?
- Another complication: the history-dependence of vegetation patterns means that historical data is needed to predict future behaviour.

Global Climate Models Approaches to Predicting Future Vegetation Rainfall Predictions for the Sahel Rainfall History in the Sahel Historical Rainfall Data Set

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Rainfall History in the Sahel

 A very severe drought occurred c. 1738-1756: a reasonable starting point for simulations is zero vegetation in 1750.



- There is very limited direct data on rainfall before 1900.
- Proxy data: (i) lake levels, esp. Lake Chad; (ii) historical chronologies, e.g. Bornu Empire; (iii) memories of local peoples.

Global Climate Models Approaches to Predicting Future Vegetation Rainfall Predictions for the Sahel Rainfall History in the Sahel Historical Rainfall Data Set

Historical Rainfall Data Set

I base my historical data set on work by Sharon Nicholson (Florida State U) on rainfall history in the Sahel.

Sahel "wetness index" 1800-2000



- Extension back to 1750 is based on historical work of Stefan Norrgård (Turku)
- Extension forwards to present is based on recent rain gauge data
- I use linear correlation of data for overlapping years to combine the data sets

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Vegetation Pattern Formation History-Dependence in Vegetation Patterns Global Climate Models and Historical Climate Data

Predicting Future Vegetation Levels Inferring the Historical Origin of Patterned Vegetation Global Climate Models Approaches to Predicting Future Vegetation Rainfall Predictions for the Sahel Rainfall History in the Sahel Historical Rainfall Data Set

Historical Rainfall Data Set



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Outline

Simulation Approach Example Simulations Classification of Vegetation Predictions on Desertification

Vegetation Pattern Formation

- 2 History-Dependence in Vegetation Patterns
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Inferring the Historical Origin of Patterned Vegetation

Inferring the Historical Origin of Patterned Vegetation

Simulation Approach

Simulation Approach Example Simulations Classification of Vegetation Predictions on Desertification

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Inferring the Historical Origin of Patterned Vegetation

Simulation Approach Example Simulations Classification of Vegetation Predictions on Desertificatior

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Simulation Approach



- I run simulations from 1750-2100
- A varies over time to reflect the historical rainfall data set, and predictions of future rainfall levels (CMIP5)

Inferring the Historical Origin of Patterned Vegetation

Simulation Approach Example Simulations Classification of Vegetation Predictions on Desertification

Simulation Approach



- I run simulations from 1750-2100
- A varies over time to reflect the historical rainfall data set, and predictions of future rainfall levels (CMIP5)
- I vary parameter values and include various levels of noise; all runs done for 27 CMIP5 datasets
 - a total of 46 000 simulations

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Inferring the Historical Origin of Patterned Vegetation

Simulation Approach Example Simulations Classification of Vegetation Predictions on Desertification

Example Simulations



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Inferring the Historical Origin of Patterned Vegetation

Simulation Approach Example Simulations Classification of Vegetation Predictions on Desertification

Classification of Vegetation



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Simulation Approach Example Simulations Classification of Vegetation Predictions on Desertification

Predictions on Desertification

Percentage of years with (almost) no vegetation Historical (1750-2012): 10% Future (2013-2100): 3.5%



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Simulation Approach Example Simulations Classification of Vegetation Predictions on Desertification

Predictions on Desertification

Percentage of years with (almost) no vegetation Historical (1750-2012): 10% Future (2013-2100): 3.5%

Relative frequencies of 1, 2, 3, ... consecutive years of desert



Simulation Approach Example Simulations Classification of Vegetation Predictions on Desertification

Predictions on Desertification

Percentage of years with (almost) no vegetation Historical (1750-2012): 10% Future (2013-2100): 3.5% Relative frequencies of 1, 2, 3, ... consecutive years of desert



Conclusion: the vast majority of simulations imply relatively high vegetation levels throughout the 21st century, with much lower levels of desertification than for the previous 2.5 centuries.

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Vegetation Pattern Formation
History-Dependence in Vegetation Patterns
Global Climate Models and Historical Climate Data
Predicting Future Vegetation Levels
Inferring the Historical Origin of Patterned Vegetation



Banded Vegetation on Slopes Mathematical Model on a Slope Wavelength vs Slope for Degradation of Uniform Vegetation Conclusions

- Vegetation Pattern Formation
- 2 History-Dependence in Vegetation Patterns
- 3 Global Climate Models and Historical Climate Data
- 4 Predicting Future Vegetation Levels

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Banded Vegetation on Slopes Mathematical Model on a Slope Wavelength vs Slope for Degradation of Uniform Vegetation Conclusions

Banded Vegetation on Slopes

On slopes, run-off occurs in one direction only, giving striped patterns parallel to the contours.



Bushy vegetation in Niger



Mitchell grass in Australia (Western New South Wales)

Banded vegetation patterns are found on gentle slopes in semi-arid areas of Africa, Australia, Mexico and S-W USA.

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Banded Vegetation on Slopes

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Mitchell grass in Australia (Western New South Wales)

Wavelength can be measured via remote sensing.

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Predicting the Future of Semi-Arid Vegetation

Banded Vegetation on Slopes Mathematical Model on a Slope Wavelength vs Slope for Degradation of Uniform Vegetation Conclusions

Data on Wavelength vs Slope

I will show that the relationship between pattern wavelength and slope provides valuable historical insights.



Data from Nevada, USA (Pelletier et al, J. Geophys. Res. 117: F04026, 2012)

Banded Vegetation on Slopes Mathematical Model on a Slope Wavelength vs Slope for Degradation of Uniform Vegetation Conclusions

The Origin of Vegetation Patterns

Vegetation patterns develop via either degradation of uniform vegetation or colonisation of bare ground

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Banded Vegetation on Slopes Mathematical Model on a Slope Wavelength vs Slope for Degradation of Uniform Vegetation Conclusions

Mathematical Model on a Slope

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Banded Vegetation on Slopes Mathematical Model on a Slope Wavelength vs Slope for Degradation of Uniform Vegetation Conclusions

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How to Predict Pattern Wavelength

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Wavelength vs Slope for Degradation of Uniform Vegetation

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Wavelength vs Slope for Degradation of Uniform Vegetation



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Wavelength vs Slope for Degradation of Uniform Vegetation



For realistic parameters, wavelength increases with slope

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Banded Vegetation on Slopes Mathematical Model on a Slope Wavelength vs Slope for Degradation of Uniform Vegetation Conclusions

Wavelength vs Slope for Colonisation



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Wavelength vs Slope for Colonisation



Wavelength decreases with slope

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Giobal Climate Models and Historical Climate Data Predicting Future Vegetation Levels Inferring the Historical Origin of Patterned Vegetation	Wavelength vs Slope for Degradation of Uniform Vegetation Conclusions
Vegetation Pattern Formation	Banded Vegetation on Slopes
History-Dependence in Vegetation Patterns	Mathematical Model on a Slope

Wavelength is positively correlated with slope ⇒ vegetation pattern originated by degradation of uniform vegetation

Wavelength is negatively correlated with slope \Rightarrow vegetation pattern originated by colonisation of bare ground

Main message: combined wavelength–slope data is much more valuable than wavelength data alone.

Banded Vegetation on Slopes Mathematical Model on a Slope Wavelength vs Slope for Degradation of Uniform Vegetation Conclusions

Example: The African Sahel



- Patterned vegetation is widespread in the Sahel
- Several studies of banded vegetation show wavelength ↓ as slope ↑

Banded Vegetation on Slopes Mathematical Model on a Slope Wavelength vs Slope for Degradation of Uniform Vegetation Conclusions

Rainfall History in the Sahel

- The Sahara and Sahel have been arid for about 5000 years, but the level of aridity has varied significantly.
- The Sahel was relatively humid in the 16th and 17th centuries.
- Reasonable assumption: areas with vegetation patterns today had uniform vegetation at the end of the 17th century.
- Since wavelength decreases with slope, my results imply that vegetation must have died out and then recolonised since the end of the 17th century.
- The most severe drought since 1700 was c. 1738-1756. So today's vegetation patterns result from recolonisation since 1760.

Vegetation Pattern Formation History-Dependence in Vegetation Patterns Global Climate Models and Historical Climate Data Predicting Future Vegetation Levels Inferring the Historical Origin of Patterned Vegetation
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List of Frames

Banded Vegetation on Slopes Mathematical Model on a Slope Wavelength vs Slope for Degradation of Uniform Vegetation Conclusions





- Rainfall History in the Sahel
- Historical Rainfall Data Set

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C MATHEMATICAL BIOLOGY, ECOLOGY AND MEDICINE

APPLICATION OF MATHEMATICS TO THE LIFE SCIENCES IS AN EXCITING AND RAPIDLY GROWING AREA OF RESEARCH THAT PROVIDES THE **OPPORTUNITY TO USE MATHEMATICS TO ANSWER QUESTIONS OF REAL** IMPORTANCE TO SOCIETY.

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