Exercises 5

- (1) (a) Write out (1 + x)⁸ using ∑-notation.
 (b) Write out (1 x)⁸ using ∑-notation.
 (c) Calculate the coefficient of a²b⁸ in (a + b)¹⁰.
 (d) Calculate the coefficient of x³ in (3 + 4x)⁶.
 (e) Calculate the coefficient of x³ in (3x² ½x)⁹. What is the value of the constant term?
- (2) Use the binomial theorem to prove the following.

 (a) $2^n = \sum_{i=0}^n \binom{n}{i}$.

 (b) $0 = \sum_{i=0}^n (-1)^i \binom{n}{i}$.

 (c) $(\frac{3}{2})^n = \sum_{i=0}^n \frac{1}{2^i} \binom{n}{i}$.